

### Colloquium, November 3, 2011 **Actually: Teaching and Researching** with Collaboration Tools and Technology



10:30 AEST Mon Nov 1 2010 Adam Bub

#### 10 images in this story

Travel experts Lonely Planet have named the top 10 cities for 2011 in their annual travel bible, Best in Travel 2011. The top-listed cities win points for their local cultures, value for money, and overall va-vavoom. So which cities make the cut? Find out here, from 10 to 1...

What do you think of the list? **Tell us here!** 

**Related links: Lonely** Planet destination videos A weekend in Newcastle Images: ThinkStock/Getaway



National eResearch Collaboration Tools and Resources Project

# Proposed NeCTAR VLs

#### Effective Teaching Effective Learning









## Effective Teaching, Effective Learning in the Quantitative Disciplines

funded by Australian Learning and Teaching Council

# Teaching with Collaboration Tools at the Tertiary Level?



Support provided by ALTC, an initiative of the Australian Government Department of Education, Employment and Workplace Relations. The views expressed in this presentation do not necessarily reflect the views of the Australian Learning and Teaching Council Ltd.

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Computer Assisted Research Mathematics and its Applications

# Actually: Teaching and Researching with Collaboration Tools and Technology.

I shall describe highlights of my two decades of experience with Advanced Collaborative Environments (ACEs) in Canada and Australia, running shared seminars, conferences, resources and courses over the internet.

### Presence at a distance

- What works
- What doesn't?
- Why?

Revised 28/09/11



CARMA's 3D Logo

# Research, Teaching & Outreach



 Are each helped by the others - and by collaborative technology - but content comes first





"Just a darn minute! — Yesterday you said that X equals two!"



- Especially teaching
- easy things
- You can't take liberties

- Technology can help
- But only so much
- Unis can't afford much

### **Technology Includes**





"It's not the math I hate...It's the aftermath."





Möbius Transfermation

Revealed



http://www.carma.newcastle.edu.au/~jb616/lm-june.htm

### All Artefacts:

- Cartoons
- Pictures
  - Films
  - Music
- Animations
- Simulations
- Spreadsheets
  - Packages
    - Applets
    - Haptics
- Virtual Reality
- <u>Blogs</u> (Math Drudge)
  - JSTOR, Amazon, iTunes...





Random walks on the first million digits of Pi (top) and e (bottom)







# That's Mathematics

Tune - "That's Entertainment

This was most likely written for the July <sup>-</sup> Fermat Fest held in San Francisco.



What's the chance it will snow

July 16, 2002

Jonathan Borwein CoLab, Dept. of Mathematics Simon Fraser University 8888 University Drive Burnaby, BC Canada V5A1S6

Dear Jonathan Borwein:

As sole copyright owner of the song THAT'S MATHEMATICS, I grant you permission to use it on the CD mentioned in your letter of July 7th, in the manner described therein.

I dare say I should charge a fee for this use, but since I assume the song is already out there on the web in mp3 form without my permission (as many of them are), I can't justify penalizing you for being honest. In other words, there will be no charge.

I own all the rights, by the way, so you don't have to clear it with Rhino. If there is to be any printed material accompanying the CD\_the credit should

read: © 1995 Tom Lehrer. U

Good luck with your project. can't determine the remaind appears on the calculator), I

Sincerely yours,

Tom Lehrer



graduates who e decimal that ation.

### SFU VR 2002: Caveman Geometry

Very cool for the one person with control and very expensive

### **Resources not Courses**?



 Current and expected advances in mathematical computation and scientific visualization make it now possible to do(teach, learn) mathematics in many varied and flexible ways.

 We'll continue to explore and flag the opportunities to integrate computational, graphic and other tools into our teaching - for philosophic, pedagogic and aesthetic reasons



THE COMPUTER AS CRUCIBLE AN INTRODUCTION TO EXPERIMENTAL MATHEMATICS

JONATHAN BORWEIN . KEITH DEVLIN

- <u>http://www.experimentalmath.info</u>
- <u>http://carma.newcastle.edu.au/portal/</u>







## "Seminars" on Hormones

- 1991-93 Internet based experience (pre WWW)
  - www.cecm.sfu.ca
- 1994-2001 PL in Canadian NCE TeleLearning
  - Multimodal Modal Mathematics (many early Applets)
  - \* 1994-6: Organic Mathematics Project (OMP)
  - AMS Notices <u>article</u> (in Press)
- 2001-03 <u>www.irmacs.sfu.ca</u>



Effective Teaching Effective Learning

- Nationally funded math-science <u>collaboration centre</u>
- 2002 SFU CoLab: my 1<sup>st</sup> <u>ACE</u> (session at ICIAM03)
- 2006 Talk on ACE-Collaboration to SSHRC
- 2003-2011 WestGrid ACE Research Project WestGrid



### Pictures in Mathematics



A heavy warning used to be given [by lecturers] that pictures are not rigorous; this has never had its bluff called and has permanently frightened its victims into playing for safety. Some pictures, of course, are not rigorous, but I should say most are (and I use them whenever possible myself). J. E. Littlewood, 1885-1977

From Littlewood's Miscellany (p. 35 in 1953 edition). Said long before the current graphic, visualization and geometric tools were available.



#### Roots of Zeros

What you draw is what you see (visible patterns in number theory)



### **Visual Theorems**



Briefly, a visual theorem is the graphical or visual output from a computer program - usually one of a family of such outputs - which the eye organizes into a coherent, identifiable whole and which is able to inspire mathematical questions of a traditional nature or which contributes in some way to our understanding or enrichment of some mathematical or real world situation. Davis et al, The Mathematical Experience, 1993, p. 333.



Roots of Zeros

What you draw is what you see (visible patterns in number theory)



### **Pictures as Datasets**



Striking fractal patterns formed by plotting complex zeros for all polynomials in powers of x with coefficients 1 and -1 to degree 18 (from <u>Organic Maths</u>)

Coloration is by sensitivity of polynomials to slight variation around the values of the zeros. The color scale represents a normalized sensitivity to the range of values; red is insensitive to violet which is strongly sensitive.

- All zeros are pictured (at 3600 dpi)
- Figure 1b is colored by their local density
- Figure 1d shows sensitivity relative to the x<sup>9</sup> term
- The white and orange striations are not understood

A wide variety of patterns and features become visible, leading researchers to totally unexpected mathematical results



#### Roots of Zeros

What you draw is what you see (visible patterns in number theory)



#### Roots in the most stable colouring







J. G. Roederer

INFORMATION AND ITS ROLE IN NATURE



The TIFF on THREE SCALES: 100, 300, 3600 dpi

Pictures are more democratic but they come from formulae



In 1995 or so Andrew Granville emailed me the number

[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, ...]

In 2008 there are at least two or three other strategies

I asked for its continued fraction? It was

 $\alpha := 1.433127426722312..$ 

I reached for a good book on continued fractions and found the answer

where Ia and I, are Bessel functions of the first kind. (Actually I knew

· Given (1), type "arithmetic progression", "continued fraction" into Google

and challenged me to identify it (our inverse calculator was new in

 L: PBB in Vancouver BC on H323

 C: Me in Newcastle NSW on Skype (both at home)

 R: Scott in Halifax NS on Access Grid

Now microseconds matter

Main Audience in **IRMACS** 100 seat passive 3D room

### **Dislocated Conferences**



2001 Many distance Seminar & Conference
 Presentations: Skype, EVO, Access Grid, H323, ...

- \* 2009 IRMACS-Fields Number Theory: shared plenaries
- \* 2011 JonFest 2011 in Vancouver: AG and streamed ...

 2005 Frequent dislocated Theses defences and Job Interviews (in many fields)

- 2005 The C2C ('coast to coast') seminar
   2008 Book chapter (on what and what not to do)
   2008 Presentation on C2C experience
  - \* 2011 6 years of <u>Remote Collaboration</u> article

2011 TransPacific Workshop regularly with UBC/SFU



COMMUNICATING MATHEMATICS IN THE DIGITAL ERA

J. M. BORWEIN, E. M. ROCHA, AND J. F. RODRIGUES

### Standards, Standards



- Uniformization only works up to a point
- Organizational and technical agility are critical

HOW STANDARDS PROLIFERATE: (SEE: A/C CHARGERS, CHARACTER ENCODINGS, IN STANT MESSAGING, ETC.)

SITUATION: THERE ARE 14 COMPETING STANDARDS.

14?! RIDICULOUS! WE NEED TO DEVELOP ONE UNIVERSAL STANDARD THAT COVERS EVERYONE'S USE CASES. YEAH!

SOON:

SITUATION: THERE ARE 15 COMPETING STANDARDS.

# **Technological Issues**



- Picking the right technology for a given setting
   Applications layers? Interactivity?
- Multi-site and band-width issues
   Decide who is the client/server
   Security issues: tests, interviews
- Sound
  - Echo cancellation/feed back
  - Questions/muting/microphones
- Images
  - Computer and/or cameras
- Avoid unnecessary bells and whistles



Technological adoption decisions are usually made by institutional ignoramuses who never have to, nor could, use the resources (from Blackboard to iPad)

# **Organizational Issues**

### Quality Assurance

- Practice sessions are key
- Rules to be followed
  - It should be 'easy as chalk' but ...
- Adequate human technical support

### Production events or one- off experiments?

- Effort to reward ratio?
- Advertise, Advertise.
  - Under promise and over deliver
- Try to store, measure and get feedback

### An HCI class ppt analysis of a CoLab Honours class, and more









## My Maths Portal

#### Jon Borwein's Mathematics Portal

The following is a list of useful math tools. The distinction between categories is somewhat arbitrary.

#### **Utilities (General)**

- 1. The On-Line Encyclopedia of Integer Sequences
- 2. ISC2.0: The Inverse Symbolic Calculator
- 3. 3D Function Grapher
- 4. Julia and Mandelbrot Set Explorer
- 5. The KnotPlot Site
- 6. The Cinderella Geometry Site

#### **Utilities (Special)**

- 7. BBP Digit Database
- 8. Integer Relations Interface: PSLQ and LLL
- 9. EZ Face: Evaluation of Euler Sums and Multiple Zeta Values
- 10. <u>GraPHedron: Automated and Computer Assisted Conjectures in Graph</u> <u>Theory</u>
- 11. <u>ProofWeb a system for teaching logic and for using proof assistants</u> through the web
- 12. Embree-Trefethen-Wright Pseudospectra and Eigenproblems
- 13. Symbolic and Numeric Convex Analysis Tools

#### Reference

- 14. NIST Digital Library of Mathematical Functions
- 15. Experimental Mathematics Website
- 16. Numbers, Constants, and Computation
- 17. Numbers: the Competition
- 18. The Prime Pages
- 19. MathResource Online Dictionary

#### Content

- 20. Math in the Media (from the AMS)
- 21. Wolfram Mathworld
- 22. Planet Math
- 23. Wikipedia: Mathematics
- 24. Euclid in Java
- 25. Finch's Mathematical Constants

#### Math Courses 2011

26. <u>MUlti Zeta Values Honours Course 2010</u> (Borwein and Zudilin) Given over the <u>AMSI Access Grid Network</u>





#### Coxeter 1930

#### **CARMA 2010**



# Workshop



### 29 - 30 September, 2011 University of Wollongong, NSW

#### Presenters

- Leigh Wood, Macquarie University
- Caz Sandison, University of Wollongong
- Walter Bloom, Murdoch University
- Jonathan Borwein, University of Newcastle
- Christine Brown, University of Wollongong
- Paul Denny, University of Auckland
- David Easdown, The University of Sydney
- Mark Nelson, University of Wollongong
- Katherine Seaton, LaTrobe University
- Shane Wilson, ING Direct Australia



#### IRMACS Opening, 2005

# Thank You